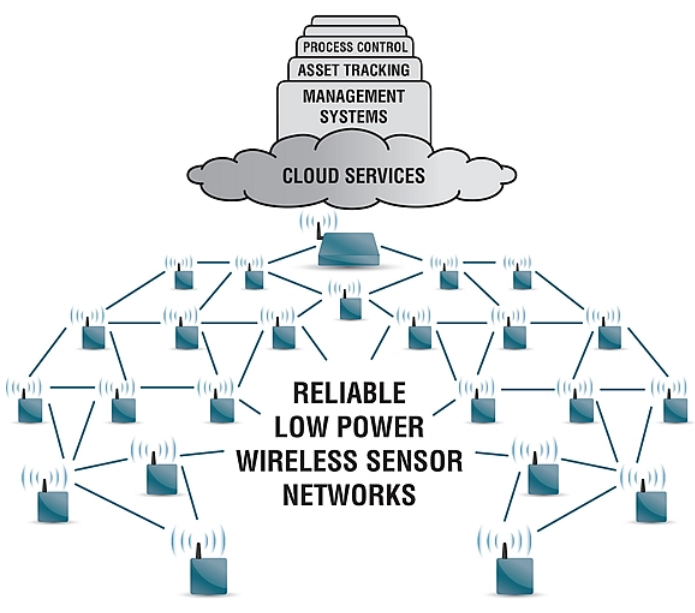


# MULTI-HOP NETWORK DESIGN UNDER IEEE 802.15.4 FOR IOT APPLICATIONS

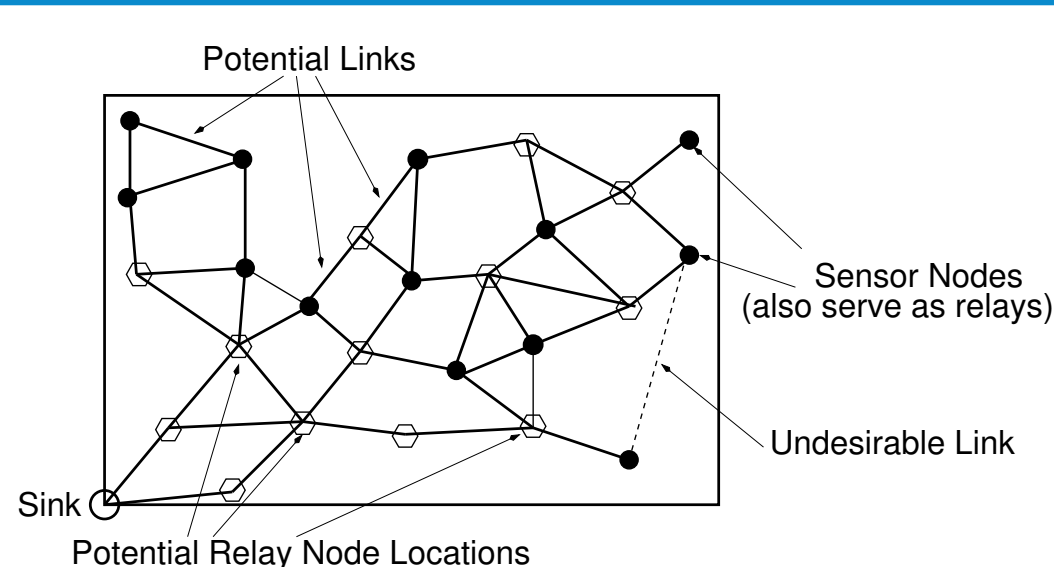
ABHIJIT BHATTACHARYA, ANURAG KUMAR

## Wireless Sensor Networks and IoT



- Wireless sensor networks essential component of the Internet of Things
- Sensor data → WSN → Gateway/sink → Internet → Cloud
- How do we design wireless networks for interconnecting sensors in the field to the Internet with some guaranteed QoS?

## The Subgraph Design Problem



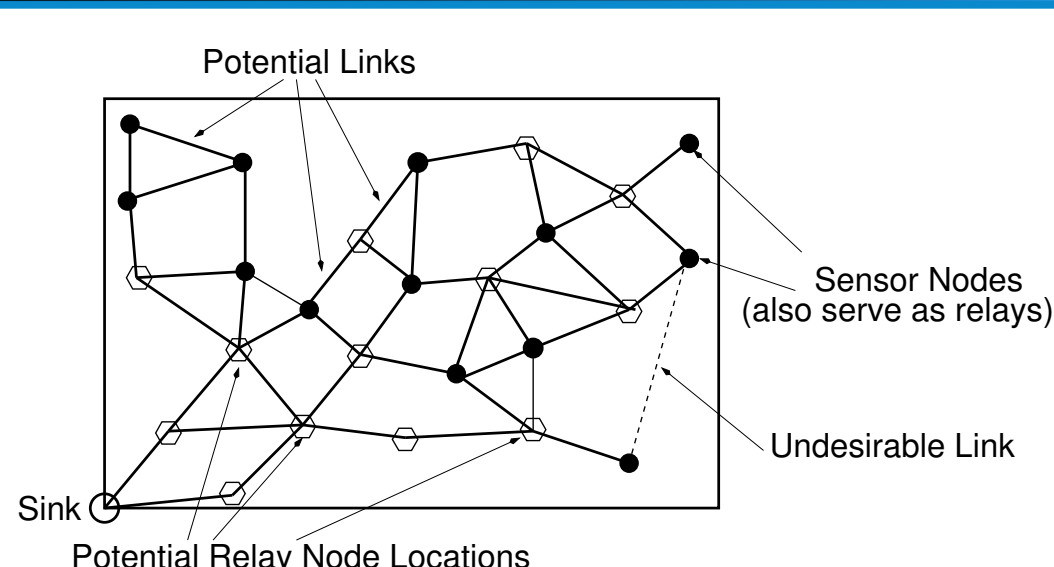
- Given: sensor locations, sink location, potential relay locations, *fixed* transmit power of the nodes
- There is a graph of “good” links
- Problem: select a set of potential relay locations to place relays
  - Obtain a multihop wireless network with some desired properties, e.g., min number of relays
  - $P[\text{end-to-end delay} \leq d_{\max}] \geq P_{\text{del}}$

## Traffic Rate Regimes

- **Very light traffic regime**
  - Environment/resource monitoring
  - Measurements required at multiple seconds or minutes
  - Essentially no inter-node contention
  - In this regime, Target  $p_{\text{del}} \Rightarrow$  Hop Constraint
- **Light to moderate traffic regime**
  - Sub-second measurement rates
  - E.g., health monitoring
  - Contention due to CSMA/CA

**Theorem:** To meet QoS target for *light to moderate* traffic regime, *necessary* to satisfy the same under *very light* traffic regime.

## Network Design for Very Light Traffic



- Given a graph over the sources, potential relay locations, and the sink
- **Problem:** Extract a subgraph spanning the sources, rooted at the sink
  - using a minimum number of relays s.t.
  - Each source is connected to the sink with hop count at most  $h_{\max}$
- **Set Cover-Hard**  $\Rightarrow$  Need **approximation algorithms**

## ILP Formulation

- $\Gamma^k$ : the set of minimal node cuts for a source node  $k$

$$\min \sum_{j \in R} y_j \quad (1)$$

$$\text{Subject to: } \sum_{j \in \gamma} y_{j,k} \geq 1 \quad \forall \gamma \in \Gamma^k; \forall k \in Q \setminus \{0\} \quad (2)$$

$$y_j \geq y_{j,k} \quad \forall j \in R; \forall k \in Q \setminus \{0\} \quad (3)$$

$$\sum_{j \in V \setminus \{k,0\}} y_{j,k} \leq h_{\max} - 1 \quad \forall k \in Q \setminus \{0\} \quad (4)$$

$$y_{j,k} \in \{0, 1\} \quad \forall k \in Q \setminus \{0\}; \forall j \in V \setminus \{k, 0\} \quad (5)$$

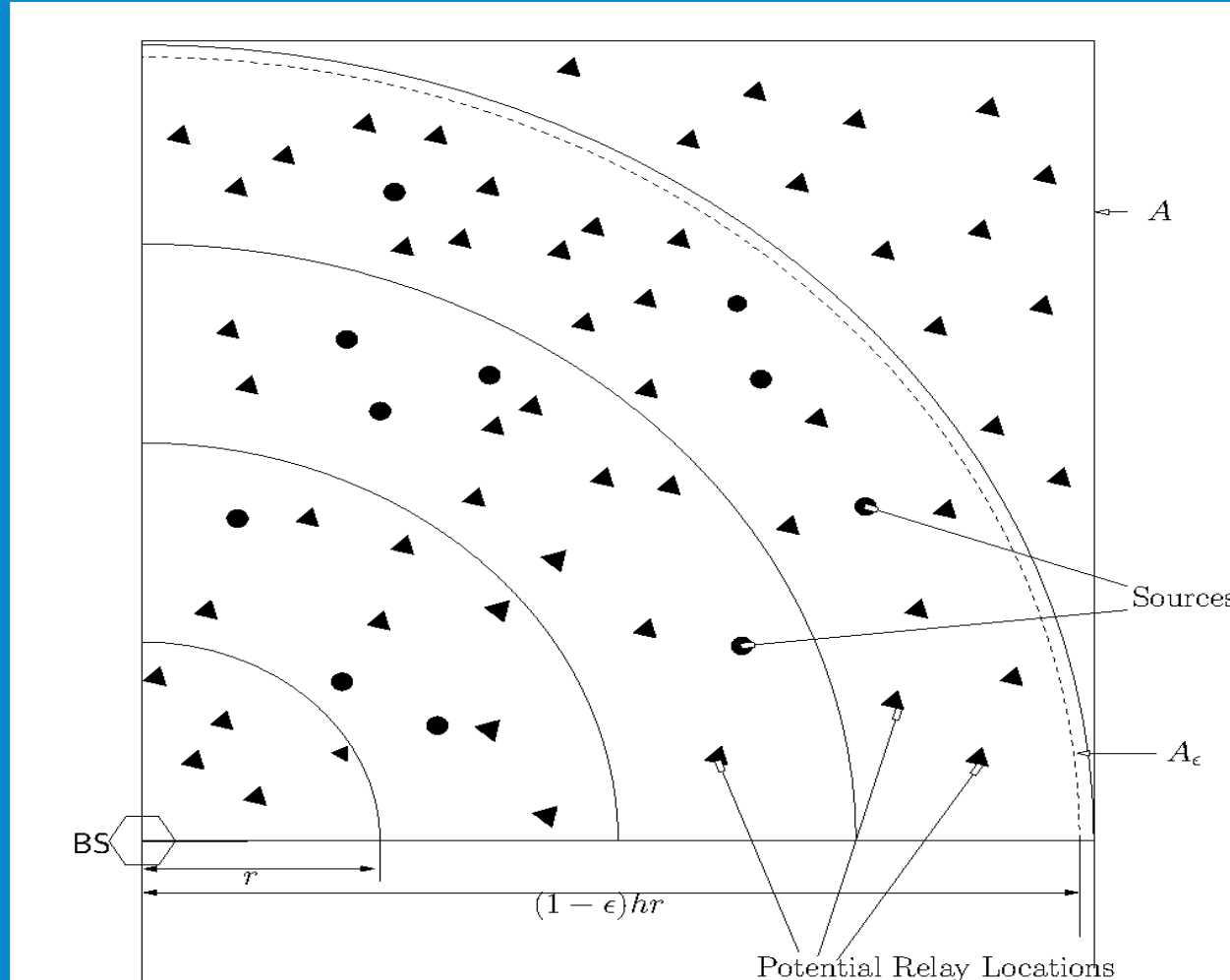
$$y_j \in \{0, 1\} \quad \forall j \in R \quad (6)$$

**Theorem:** Opt. value of the objective function for the ILP = Opt. solution to the design problem

## Poly-time Heuristic

- Sequence of shortest path computations from the sources to the sink
  - Start with a **shortest path tree (SPT)** on the entire network graph
    - \* Any source-sink path longer than  $h_{\max} \Rightarrow$  problem infeasible
  - Prune relay nodes from the feasible solution sequentially
  - Each time, compute a new SPT over only the remaining nodes
  - Until hop constraint is violated
- **Empirical** average case approx. ratio close to 1 from over 1000 randomly generated scenarios
- **Theorem (Worst case approx. ratio):**  $\min\{m(h_{\max} - 1), (|R| - 1)\}$ , where  $m = \#$  sources,  $h_{\max} =$  hop constraint, and  $|R| = \#$  potential relay locations
  - Too conservative

## Average Case Analysis: Setting



- $n$  potential locations i.i.d. uniformly over  $A$
- $m$  sources i.i.d. uniformly over  $A_\epsilon$
- Yields  $\mathcal{G}^r(\omega)$ : RGG consisting of links of length  $\leq r$
- $\mathcal{X} = \{\omega : \omega \text{ is hop count feasible}\}$
- For  $n \geq n_0(\epsilon, \delta, h_{\max}, r)$ ,  $Pr[\mathcal{X}] \geq 1 - \delta$
- $N_{\text{algo}}(\omega)$ : # relays in the outcome of the algorithm on  $\mathcal{G}^r(\omega)$
- $R_{\text{opt}}(\omega)$ : # relays in an optimal solution to the design problem on  $\mathcal{G}^r(\omega)$
- Define **average case approximation ratio**

$$\alpha \triangleq \frac{E[N_{\text{algo}}|\mathcal{X}]}{E[R_{\text{opt}}|\mathcal{X}]}$$

## Average Case Analysis: Results

**Lemma 1:**

$$E[N_{\text{algo}}|\mathcal{X}] \leq m \left[ h_{\max} - \frac{1}{(1-\epsilon)^2 h_{\max}^2} - \sum_{j=2}^{h_{\max}-1} \frac{j^2}{h_{\max}^2} \right] - m + m\delta(h_{\max} - 1) \triangleq \bar{N}$$

**Lemma 2:**

$$E[R_{\text{opt}}|\mathcal{X}] \geq \left[ 1 - \left( \frac{h_{\max} - 1}{(1-\epsilon)h_{\max}} \right)^{2m} \right] (1-\delta) \sum_{i=1}^{h_{\max}-1} \left( 1 - \frac{n_i^2}{(1-\epsilon)^2 h_{\max}^2} \right)^{m-1} \triangleq \underline{R}_{\text{opt}}$$

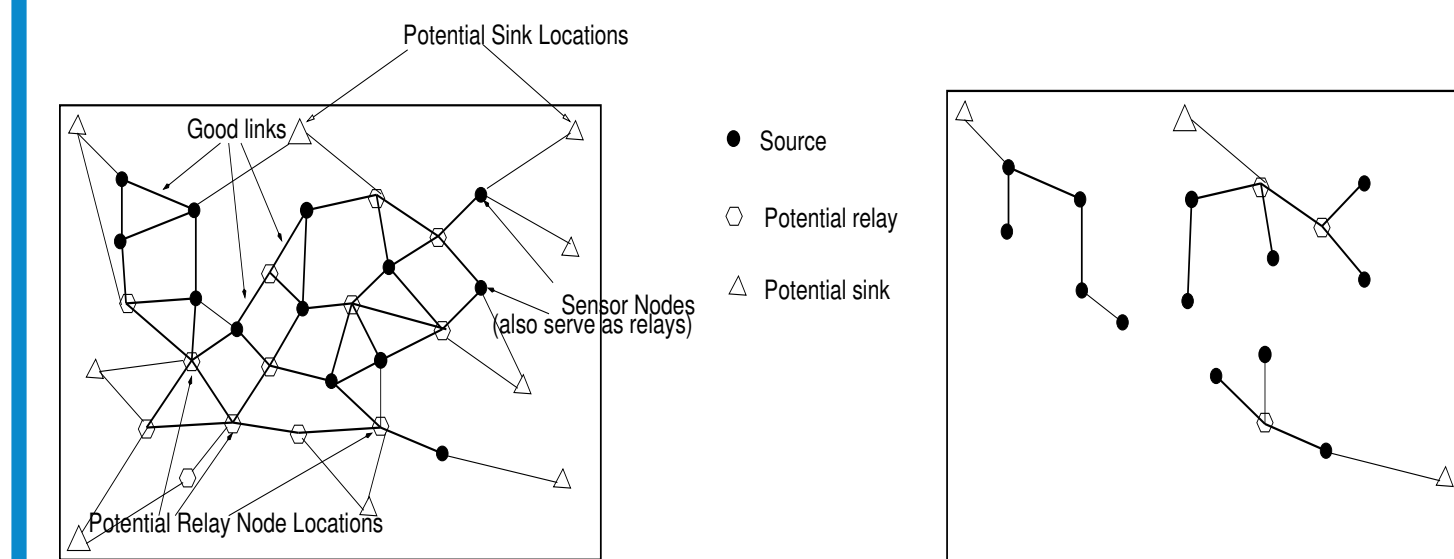
where,  $n_i = \min(i, h_{\max} - i)$

**Theorem:** Average case approx. ratio,  $\alpha \leq \frac{\bar{N}}{\underline{R}_{\text{opt}}}$

## References

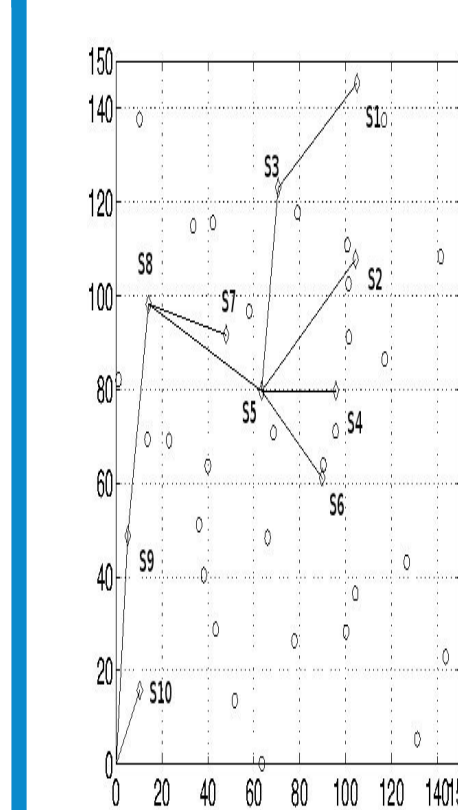
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## Multi-Sink Network Design



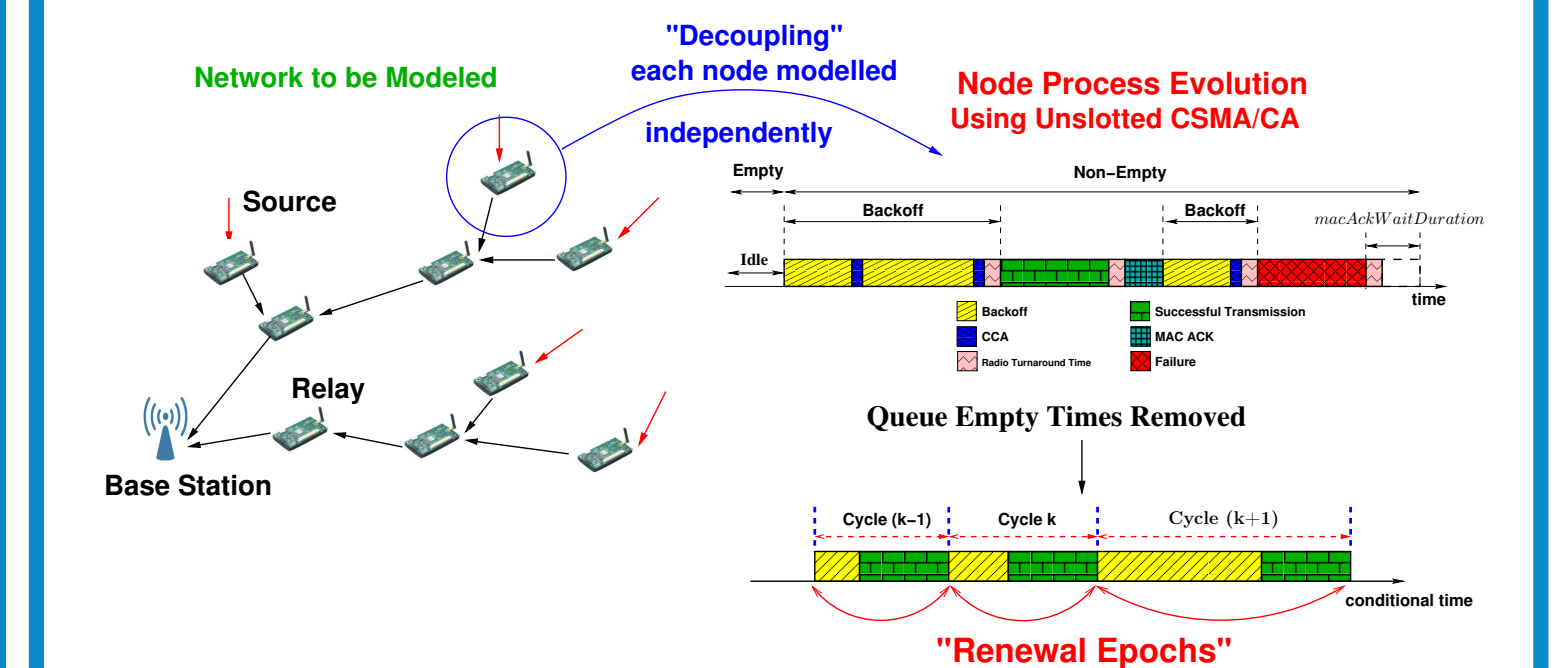
- Cost of each *potential* sink location,  $c_s$
- Cost of each *potential* relay location,  $c_r$
- **Problem:** Extract a subgraph spanning the sources
  - using a minimum cost selection of relays and sinks s.t.
  - each source has a path to at least one sink with hop count at most  $h_{\max}$
- **Set Cover Hard**; we employ a set cover based greedy heuristic
- Fast run-time; close to optimal solutions in practice

## Beyond Very Light Traffic



- A **very light traffic** design
- Hop counts  $h_i, 1 \leq i \leq m$ , being bounded by  $h_{\max}$  ( $= 5$  in the example)
- Measurement generation rate at sensors  $\lambda$  pkts/s
- **Find largest  $\lambda$  s.t. packet drop probability at a link is at most a target  $\bar{\delta}$**
- Develop an analytical model for IEEE 802.15.4 CSMA/CA multihop networks
- Use the model to obtain constraints on arrival rates and topology to meet QoS

## 802.15.4 CSMA/CA Network Analysis



- **Decoupling:** Stochastic process at each node modeled independently, isolating it from the rest of the network
  - treating the rest of the network as environment
  - environment modeled by its unknown time averaged statistics
- **Recoupling:** The individual node processes are coupled via fixed point equations involving their unknown time averaged statistics

## Fixed Point Eqns.: No Hidden Nodes

$$\eta_i = \frac{\beta_i}{\beta_i + \sum_{j \neq i} \bar{\tau}_j^{(i)}}; c_i = \left( 1 - e^{-12 T_s \beta_i} \right)$$

$$\bar{\tau}_j^{(i)} = \frac{\beta_j \times b_j \times q_j}{1 - q_j + q_j \times b_j}; \gamma_i = l + (1 - l)p_i$$

$$\alpha_i = \frac{\eta_i + (1 - \eta_i)c_i + (1 - \eta_i)(1 - c_i)\beta_i T_{tx}}{\eta_i + (1 - \eta_i)c_i + (1 - \eta_i)(1 - c_i)\beta_i T_{tx}}$$

$$p_i = \frac{R_i^{(3)} + R_i^{(4)}}{\eta_i + (1 - \eta_i)c_i}; R_i^{(4)} = (1 - \eta_i)c_i$$

$$R_i^{(3)} = \eta_i \left( 1 - \exp \left\{ -12 T_s \left( \sum_{j \neq i} \bar{\tau}_j^{(i)} \right) \right\} \right)$$

$$\bar{B}_i = 78 + 158\alpha_i + 318\alpha_i^2 + 318\alpha_i^3 + 318\alpha_i^4; r_i = \gamma_i(1 - \alpha_i^5)$$

$$\bar{Z}_i = \bar{B}_i(1 + r_i + r_i^2 + r_i^3)$$

$$\bar{Y}_i = (1 - \alpha_i^5)T(1 + r_i + r_i^2 + r_i^3)$$

$$\frac{1}{\sigma_i} = \bar{Z}_i + \bar{Y}_i; b_i = \frac{\bar{B}_i}{\bar{B}_i + (1 - \alpha_i^5)T_{tx}}$$

$$\beta_i = \frac{1 + \alpha_i + \alpha_i^2 + \alpha_i^3 + \alpha_i^4}{\bar{B}_i}$$

$$q_i = \frac{\nu_i}{\sigma_i}; \nu_i = \lambda_i + \sum_{k \in \mathcal{P}_i} \theta_k; \theta_k = \nu_i(1 - \delta_i)$$

$$\delta_i = \alpha_i^5(1 + r_i + r_i^2 + r_i^3) + r_i^4$$

## Light Traffic Design: NH Nodes

- For the light traffic regime, we obtain a design constraint

$$\lambda \sum_{i=1}^m h_i \leq B(\bar{\delta}, T)$$

- $T =$  packet duration;  $B(\cdot, \cdot)$  has an explicit formula
- Taylor expansion around the detailed fixed point  $\Rightarrow$  simpler scalar fixed point
- The scalar f.p. analyzed using monotonicity arguments, and concepts from Real Analysis (Lipschitz continuity, contraction principle, Mean Value Theorem)

- Notice that  $\lambda \sum_{i=1}^m h_i$  is the total offered packet rate that the medium must carry
- **Example:** For default protocol parameters, with  $T = 262$  symbols, and  $\bar{\delta} = 2\%$ , we get  $B(\bar{\delta}, T) = 95.2$  packets/sec
- **Consequence:** A Shortest Path Tree is **approximately throughput optimal**